

Accurate Estimates Without Calibration?

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Abstract. Most process models calibrate their internal settings using historical data. Collecting such data collection is an expensive, tedious, and often incomplete process. Hence, we seek an alternative to calibration from historical data. Formally, historical data offers constraints to a set of model options. An alternative methods of generating those constraints is to augment a process model with a search engine (simulated annealing plus variable ranking) that finds options that improve the process model outputs. The improvements can be dramatic: in one of the studies in this paper, the search engine found process options that reduced the median and variance of the effort estimates by a factor of 20. In ten case studies, we show that the estimates generated in this manner can be quite accurate, despite being generated *without* using historical data.

1 Introduction

Without precise knowledge from an organization, it is difficult to make precise estimates about software processes at that site. For example, initial development effort estimates may be incorrect by a factor of four [4] or even more [12].

It can be very difficult to find relevant data within a single organization to fully specify all the internal parameters inside a process model. For example, after 26 years of trying, we have only collected less than 200 sample projects for the COCOMO database. There are many reasons for this, not the least being the business sensitivity associated with the data. Therefore, in this paper, we explore what can be decided from process models *without* local data.

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For this experiment, we adopt the following framework. We say that a process model P yields estimates from a combination of *Project* and *Model* variables:

$$estimates = P(Project, Model)$$

P describes the space of influences between variables. and may take many forms including discrete-event models [11, 14]; system dynamics models [1]; state-based models [2, 8, 18]; rule-based programs [22]; standard programming constructs such as those used in Little-JIL [6, 25]; or the linear models used in COCOMO [4, 5], PRICE-S [23] and SEER-SEM [10]. The strength of each influence is controlled by the *Model* variables. Taken together, the process model P and the *Model* variables store what we've learned from the past. The *Project* variables, on the other had, represent some new situation that should be analyzed using the past knowledge. For example, P could assert that “ $effort \propto pcap$ ” (programmer skills is proportional to development effort) while *Model* could contain the precise proportionality constant of -0.7 (i.e. “ $effort = -0.7pcap$ ”). Finally, *Project* could assert that programmer skills are “in the upper range”; e.g. for a COCOMO model “ $pcap \in \{4, 5\}$ ”.

We say *Project* and *Model* variables can be:

- *fixed* to one value such as “programmer capability ($pcap$) is nominal”;
- *free* to take on any legal value. In COCOMO, if $pcap$ is free, then it can takes values

$$\{veryLow = 1, low = 2, nominal = 3, high = 4, veryHigh = 5\}$$

- or *float* to some subset of the whole range. For example, a manager might declare that “our programmers are in the upper ranges”; i.e. this $pcap$ floats in a particular part of the entire $pcap$ range ($pcap \in \{4, 5\}$).

The range of legal values for variables increases from *fixed* to *float* to *free*:

$$(|fixed| = 1) < |float| < |free|$$

This paper reports an experiment that frees *both* the *Model* and *Project* variables. At first glance, such an experiment may seem perverse, particularly if the goal is to reduce uncertainty. Free variables range over a larger space than fixed variables: the more free variables, the wider the range of *Estimates*. If we free both *Model* and *Project* variables then, surely, this will result in greater *Estimate* uncertainty?

However, our analysis is not just some passive observer of a large space of options. Instead, it is an active agent that seeks parts of the options space where predictions can be made with greater certainty. We augment a Monte Carlo analysis with two tools. SA is a *simulated annealing algorithm* that minimizes *Estimates*. RANKER is a *variable pruning algorithm*, that seeks the *smallest* number of *Project* variables that *most* reduce the *Estimates*. The combination of SA+RANKER is called STAR⁴. Since it knows the most influential *Project* ranges, STAR can discover (and then constrain) the factors that most most impact *Estimates*.

⁴ The name is a geek joke. In regular expressions, the star meta-character “*” matches any characters. That is, just like STAR, it can be used to search a wide range of options.

case study	Monte Carlo	STAR
	SCAT	STAR
flight	712	44
ground	389	18
OSP	629	68
OSP2	84	31

Fig 1a: variance, in months.

case study	Monte Carlo	STAR
	SCAT	STAR
flight	1357	86
ground	737	38
OSP	1951	410
OSP2	297	182

Fig 1b: median, in months.

Fig. 1. Effort estimates seen in 1000 simulations of the *Project* ranges found by STAR. “Variance” (left hand side) shows the difference between the 75th and 50th percentile. “Median” (right hand side) shows the 50th percentile estimate.

When compared to state-of-the-art process models, the effects of a STAR-style analysis are quite dramatic. Figure 1 compares STAR’s estimates to those generated by SCAT [15–17], a COCOMO-based tool used at NASA’s Jet Propulsion Laboratory. SCAT fixes *Model* and perform a Monte Carlo simulation of the *Project* ranges. Each row of Figure 1.A is one case study:

- *flight* and *ground* systems software from NASA’s Jet Propulsion Laboratory;
- *OSP* is the GNC⁵ for NASA’s Orbital Space Plane (prototype);
- *OSP2* is a newer version of OSP.

Note that, for all four case studies, STAR reduces the variance and median estimates to a small fraction of SCAT’s estimates, sometimes as much as a factor of 20 (in Figure 1a: $\frac{712}{44} \approx 20$; in Figure 1b: $\frac{737}{38} \approx 20$).

The rest of this paper describes STAR. We extend prior work in two ways. Prior reports on STAR [20] were based on limited case studies; here we report ten new case studies showing that our main effect (reduced median and variance) holds in a wide range of cases. Also, prior reports on Figure 1 [19] failed to check the validity of those results. The ten case studies discussed below show that STAR’s estimated are quite accurate, despite being generated from a large space of *Project* and *Model* options. This validity check greatly increases our confidence in the STAR method.

2 STAR

STAR’s current implementation explores three software process models:

- The COQUALMO software defect predictor [5, p254-268].
- The COCOMO software effort predictor [5, p29-57].
- The THREAT predictor for project effort & schedule overrun [5, 284-291].

COQUALMO models two processes (defect introduction and defect removal) for three phases (requirements, design, coding). COCOMO assumes that effort is exponentially proportional to some *scale factors* and linearly proportional to some *effort*

⁵ GNC= guidance, navigation, and control

multipliers. COCOMO estimates are development months (225 hours) and includes all coding, debugging, and management activities. The THREAT model contains a large set of two-dimensional tables representing pairs of variable settings are problematic. For example, using the *rely* vs *sced* table, the THREAT model would raise an alert if our tool decides to build a system with high *rely* (required reliability) and low *sced* (schedule available to the development).

STAR samples the space of possible models inside COCOMO and COQUALMO using the following technique. Internally, COCOMO and COQUALMO models contain many linear relationships. Nominal values of $x = 3$ change some estimate by a factor of one. These COCOMO lines can hence be modeled as a straight line $y = mx + b$ passing through the point $x, y = 3, 1$. Such a line has a y-intercept of $b = 1 - 3m$. Substituting this value of b into $y = mx + b$ yields $y = m(x - 3) + 1$. COCOMO's effort slopes are either positive or negative, denoted m^+ , m^- (respectively):

- The positive slopes m^+ represents the variables that are proportional to effort; e.g. *increasing* required reliability also *increases* the development effort.
- The negative slopes m^- represents the variables that are *inversely* proportional to effort; e.g. *increasing* analyst capability *decreases* the development effort.

Based on decades of experiments with calibrating COCOMO models, we have identified variables with different slopes. These following COCOMO variables have m^+ slopes: *cplx*, *data*, *docu*, *pvol*, *rely*, *ruse*, *stor*, and *time*. Also, these variables have m^- slopes *acap*, *apex*, *ltex*, *pcap*, *pcon*, *plex*, *sced*, and *site* (for an explanation of those terms, see Figure 2). Further, based on decades of calibration of COCOMO models, we assert that effort estimation, m^+ and m^- have the ranges:

$$\begin{aligned} -0.178 \leq m^- \leq -0.078 \\ 0.073 \leq m^+ \leq 0.21 \end{aligned} \tag{1}$$

Using an analogous procedure, it is possible to derive similar equations for the COCOMO scale factors, the COQUALMO scale factors/effort multipliers/ defect removal variables (for full details, see [20]).

With the above machinery, it is now possible to define a Monte Carlo procedure to sample the space of possible THREAT/COCOMO/COQUALMO *Models*: just randomly selecting $\{m^-, m^+\}$. As to sampling the space of possible THREAT models, this is achieved by adding random variables to the cells of THREAT's tables.

STAR tries to minimize defects (D), threats (T), and development effort (E). This is a non-linear optimization function: e.g. reducing costs can introduce more defects. For this reason, we use simulated annealing (SA) to explore trade-offs between models. SA is best explained in comparison to the Metropolis algorithm.

A *Metropolis* Monte Carlo algorithm [21] improves on basic Monte Carlo as follows. New solutions are created by small mutations to some *current* solutions. In the case of STAR, an "solution" is some randomly selected part of the space of possible *Projects*. If a new solution is "better" (as assessed via an *energy function*), it becomes the new *current* solution used for future mutations. STAR's energy function is $E = \sqrt{\overline{E}^2 + \overline{D}^2 + \overline{T}^2} / \sqrt{3}$ where \overline{x} is a normalized value $0 \leq \frac{x - \min(x)}{\max(x) - \min(x)} \leq 1$. Energy ranges $0 \leq E \leq 1$ and *lower* energies are *better*. If a new solution does not

		strategic?	tactical?
scale factors (exponentially decrease effort)	prec: have we done this before?	✓	
	flex: development flexibility		✓
	resl: any risk resolution activities?		✓
	team: team cohesion		✓
	pmat: process maturity	✓	
upper (linearly decrease effort)	acap: analyst capability	✓	
	pcap: programmer capability	✓	
	pcon: programmer continuity	✓	
	aexp: analyst experience	✓	
	pexp: programmer experience	✓	
	ltex: language and tool experience	✓	
	tool: tool use		✓
	site: multiple site development	✓	
sced: length of schedule		✓	
lower (linearly increase effort)	rely: required reliability		
	data: secondary memory storage requirements		✓
	cplx: program complexity		✓
	ruse: software reuse		✓
	docu: documentation requirements		✓
	time: runtime pressure		
	stor: main memory requirements		✓
pvol: platform volatility			
COQUALMO defect removal methods	auto: automated analysis	✓	✓
	execTest: execution-based testing tools	✓	✓
	peer: peer reviews	✓	✓

Fig. 2. The variables of COCOMO, COQUALMO, and the THREAT model.

have lower energy, a Boltzmann acceptance criteria is used to probabilistically decide to assess the new state: the worse the new state, the less likely that it becomes the new current state.

A *simulated annealer* (SA) [13] adds a “temperature” variable to the Boltzmann accept criteria such that, at high temperatures, it is more likely that the algorithm will jump to a new worst current state. This allows the algorithm to jump out of local minima while sampling the space of options. As the temperature cools, such jumps become less likely and the algorithm reverts to a simple hill climber.

Our *RANKER* algorithm instruments the internals of SA. Whenever a solution is assigned some energy, that energy is added to a counter maintained for each variable setting in *Projects*. When SA terminates, *RANKER* sorts all variable ranges by the sum of the energies seen during their use. The ranges that are lower in the sort order are associated with lower energy solutions; i.e. lower defects, efforts, threats. *RANKER* then conducts experiments where it fixes the first N ranked ranges and lets the remaining variables float. N is increased till some minimum energy point is reached. A *policy* are the project settings that achieve that minimum energy point.

The last two columns of Figure 2 show the results of Delphi panel session at JPL where the COCOMO variables were separated into those *tactical* variables that can be changed within the space of one project, and those *strategic* variables that required higher-level institutional change (and so may take longer to change). For example, the panel declared that *pmat* (process maturity) is hard to change within the space of a

project	float		fixed	
	variable	low high	variable	setting
OSP	prec	1 2	data	3
	flex	2 5	pvol	2
	resl	1 3	rely	5
	team	2 3	pcap	3
	pmat	1 4	plex	3
	stor	3 5	site	3
	ruse	2 4		
	docu	2 4		
	acap	2 3		
	pcon	2 3		
	apex	2 3		
	ltex	2 4		
	tool	2 3		
	sced	1 3		
	cplx	5 6		
KSLOC	75 125			
OSP2	prec	3 5	flex	3
	pmat	4 5	resl	4
	docu	3 4	team	3
	ltex	2 5	time	3
	sced	2 4	stor	3
	KSLOC	75 125	data	4
			pvol	3
			ruse	4
			rely	5
			acap	4
			pcap	3
			pcon	3
			apex	4
			plex	4
			tool	5
		cplx	4	
		site	6	

project	float		fixed		
	variable	low high	variable	setting	
flight	rely	3 5	tool	2	
	data	2 3	sced	3	
	cplx	3 6			
	time	3 4			
	stor	3 4			
	acap	3 5			
	apex	2 5			
	pcap	3 5			
	plex	1 4			
	ltex	1 4			
	pmat	2 3			
	KSLOC	7 418			
	ground	rely	1 4	tool	2
		data	2 3	sced	3
		cplx	1 4		
time		3 4			
stor		3 4			
acap		3 5			
apex		2 5			
pcap		3 5			
plex		1 4			
ltex		1 4			
pmat		2 3			
KSLOC		11 392			

Fig. 3. Four case studies.

single JPL project. In the sequel, all our RANKER experiments will be divided into those that just use the *strategic* variables and those that just use the *tactical* variables⁶.

3 Experiments

Figure 3 shows various *Projects* expressed in term of *floating* and *fixed* variables. For example, with JPL’s flight systems, the *rely* (required reliability) can float anywhere in the upper range; i.e. $rely \in \{3, 4, 5\}$. However, for flight systems, *sced* (schedule pressure) is tightly defined (so *sced* is fixed to the value 3).

Figure 4 and Figure 5 shows the results of STAR. The variable ranges are sorted along the *x*-axis according the order generated by RANKER. At any *x* value we see the results of fixing the ranges $1..x$, letting all ranges $x + 1..max$ float, then running 1000 Monte Carlo simulations. In the results, “median” refers to the 50th percentile band

⁶ Note that these definitions of *strategic* and *tactical* choices are not hard-wired into STAR. If a user disagrees with our definitions of strategic/tactical, they can change a simple configuration file.

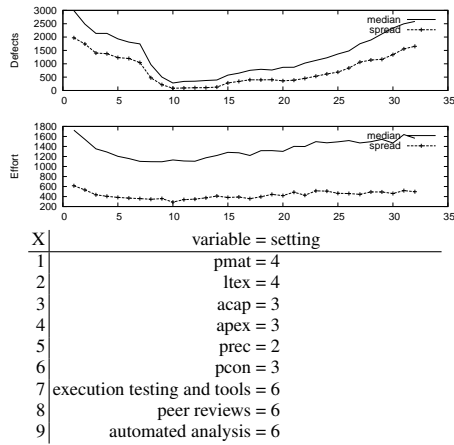


Fig. 4.A: controlling only strategic *Project* variables

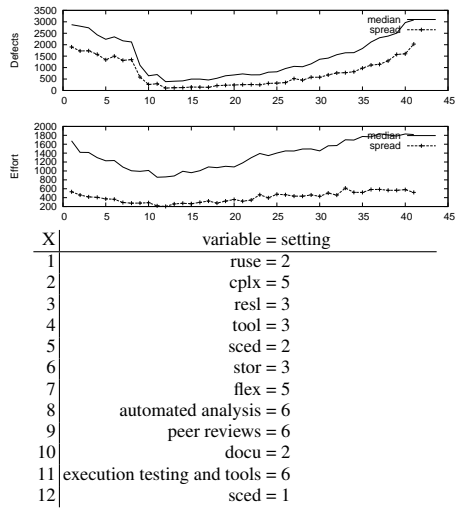


Fig. 4.B: controlling only tactical *Project* variables

Fig. 4. Some RANKER results on OSP. The settings shown under the plots describe the policy that leads to the policy point.

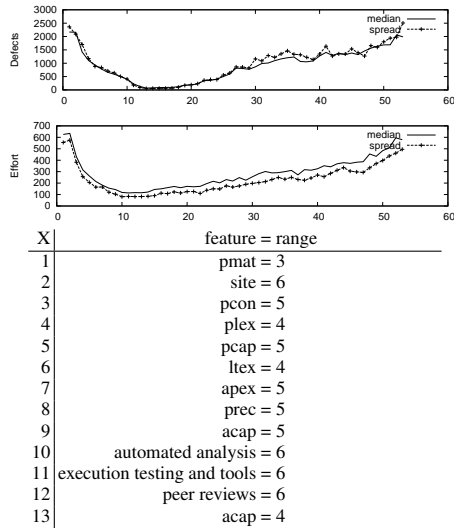


Fig. 5.A: controlling only strategic *Project* variables

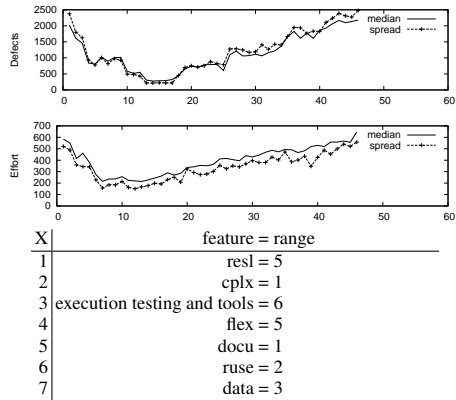


Fig. 5.B: controlling only tactical *Project* variables.

Fig. 5. Some RANKER results on JPL ground systems. The settings shown under the plots describe the policy that leads to the policy point.

and “spread” refers to the difference between the 75th and 50th percentile in the 1000 generate estimates.

For this paper, we ran SA+RANKER on the four case studies of Figure 3, plus a fifth study called “ALL” that used the entire COCOMO ranges, unconstrained by a particular project. Each study was repeated twice- one for controlling just the strategic variables and once for controlling just the tactical variables. This resulted in ten experiments.

Some of the results from four of those experiments are shown in Figure 4 and Figure 5 (space restrictions prevent us from showing all the results). In those four experiments (and in the other six, not shown) the same effect was observed. Minimum effort and defects was achieved after fixing a small number of *Project* variables (in Figure 4.A, Figure 4.B, Figure 5.A, and Figure 5.B, that number was at $X=\{9,12,13\}$ respectively). At these minimum points, the median and spread estimates were greatly reduced. We call this minimum the *polycypoint* and use the term *policy* to refer to the intersection of the case study defined in Figure 3, and the ranges found in the range between $\{1 \leq x \leq \text{polycypoint}\}$.

In terms of controlling uncertainty, the reduction in the spread estimates at the policy point is particularly interesting. Note that this reduction in model uncertainty was achieved by only controlling a few of the *Project* variables while letting all other *Project* and *Model* variables float free. That is, in these case studies, projects could be controlled (development effort and defects reduced) without using historical data to constrain the *Model* variables.

Figure 7 compares the policy point estimates with the estimates generated by standard methods. For each of our ten experiments, a set of random *Projects* were generated, consistent with the policies; i.e.

- If the policy fixes a value, then the *Project* contains that value;
- Otherwise, if the variable is found Figure 3, it is drawn from those constraints;
- Otherwise, the variable’s value is selected at random from background knowledge of the legal range of the Figure 2 variables.

For each set, the following procedure was repeated 20 times. Ten examples were removed at random and Boehm’s local calibration (LC) procedure [4, p526-529] was used to train a COCOMO model on the remaining *Project* examples⁷. LC’s estimates were then compared to the estimates generated by STAR’s simulation at the policy point (i.e. floating over both the policy and the *Model* ranges). Values were compared using $\delta = (\text{estimate}(lc) - \text{estimate}(STAR)) / \text{estimate}(LC)$. The differences found in this way are called $\Delta_1 = \sum \delta$ and are summarized in Figure 6.

The median Δ_1 values of Figure 6 is around 0.5; i.e. a STAR estimate of 100 months could really range for 50 to 150 months. Compared to the effort estimate reductions shown in the introduction, Δ_1 is quite small. Recall that STAR reduced effort estimates to a small part of the initial values, sometimes a factor of 20; i.e by a factor that is much

⁷ LC was chosen since, in extensive experiments, we have found this decades old procedure to be remarkably competitive with current data mining methods [9] including bagging and boosting [3].

median δ	case study	control method
29	OSP	strategic
33	OSP2	tactical
36	flight	tactical
41	OSP	tactical
41	flight	tactical
46	All	strategic
47	OSP2	strategic
55	ALL	tactical
56	ground	strategic
65	ground	tactical

Fig. 6. Median difference between effort estimates generated by conventional means (LC) and STAR.

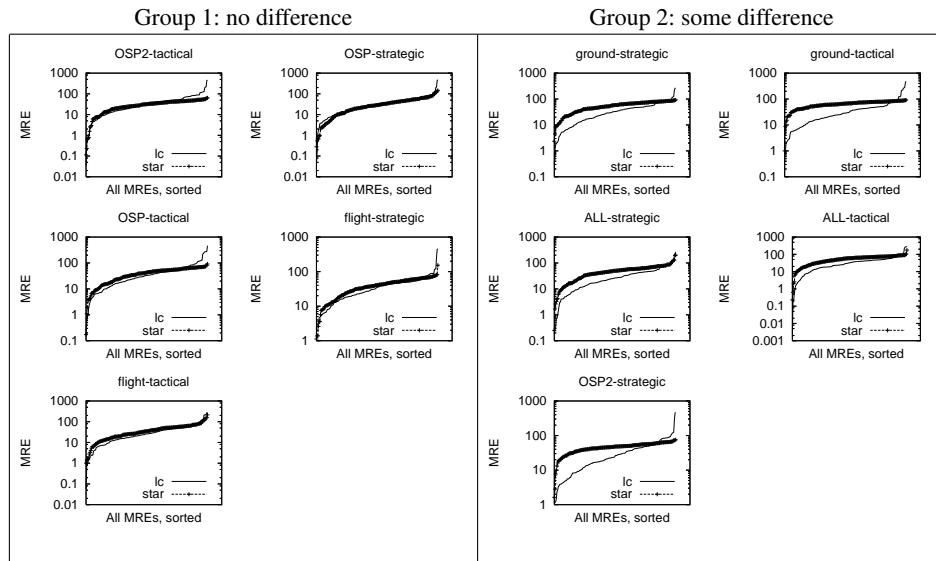


Fig. 7. Results. Divided by Mann-Whitney tests (95 and 99% confidence level). In Group 1 (left-hand-side), Mann-Whitney reports that the two sets δ in each plot are *not* statistically different. In Group 2 (right hand side), Mann-Whitney reports that δ are different. For a precise statistical comparison, see Figure 8.

		search bias	
		strategic	tactical
cast study	ground	66% ○ ●	63% ○ ●
	all	91% ● ○	75% ● ○
	OSP2	99% ● ○	125%
	OSP	112%	111%
	flight	101%	121%

Fig. 8. Differences between the sum of MREs seen with LC and STAR: table shows the calculation $\frac{\sum \delta(LC)}{\sum \delta(STAR)}$. The symbols “○” and “●” denote a statistical difference at the 95 and 99% confidence level (Mann-Whitney).

larger than 0.5. Clearly, even if STAR is wrong by $\pm 50\%$, then the overall benefits to be gained from applying STAR’s policies are still dramatically large.

Also, the Δ_1 values need to be baselined against some other method Δ_0 . Without such a baseline, we don’t know if a difference of (say) 0.5 is larger, smaller, or similar to the errors seen via other methods. Figure 7 sorts all the deltas seen in Δ_1 and compares those to the sorted deltas seen when local calibration trained and tested on the data used to compute Δ_1 . Visually, the plots seem very similar.

Statistical tests confirm the visual intuition of Figure 7 that the δ figures generated by STAR and conventional methods are very similar. In five of our ten cases, there was no significant difference between the two populations. In two of the remaining, the differences were very similar (within 91% to 99%) of each other. In the remaining cases, the difference in the discrepancy between predicted and expected was 63%, 66%, and 75%. Once again:

- Given all the randomized exploration STAR performs over the space of possible *Models*, this discrepancy is very small.
- These discrepancies are dwarfed by the much larger effort reductions of Figure 1.

4 Conclusion

In studies with one widely-used suite of effort/ detect/ threat predictors for software systems, we have shown that:

- *Estimation* median values can be greatly reduced (see Figure 1). In comparisons with other effort estimation tools, the reduction can quite dramatic. In the best case our tools found *Project* ranges that yields estimates that were 5% of estimates found by other means.
- *Estimation* variance can be reduced by only floating the *Project* values and leaving the *Model* values free (see Figure 4 and Figure 5).
- Within the space of *Project* options that most reduce *Estimation* median and variance, the predictions made by our process models are remarkably similar to those made by conventional methods (see Figure 6 and Figure 8).

The first result suggests that it may be highly advantageous to use STAR. Projects designed around STAR's recommendations will be delivered sooner and have fewer bugs or threats.

The second result is of much practical importance since it means we do not require calibration data to tune the *Model* variables. If process models can be deployed without calibration, then they can be used with much greater ease and *without* the requirement for an expensive and time-consuming period of data collection.

The third result is showing that (a) this method can find and remove the major sources of uncertainty in a project; (b) in the reduced space, it is possible to make accurate *Estimates*.

Finally, we comment on the external validity of these results. Compared to many other process models⁸ this combination of effort/threat/defect models is relatively simple. As model complexity grows, then the space of possible *Estimates* can grow exponentially and STAR's controlling effect may disappear. Therefore it is clear that we can not claim that, for *all* process models, that *Estimate* variance can be controlled by just constraining *Project*, not *Model*, variance.

On the other hand, researchers in planning and theorem proving have recently shown that as model complexity grows, other constraining effects may appear such as "master variables"; i.e. a small number of settings that control all other settings [7, 24]. Such master variables can greatly reduce the search space within large models.

In summary, it is an open issue if our results apply to other process models. Nevertheless, data collection for the purposes of model calibration is an expensive, tedious, and often incomplete process. Our results suggest that such data collection may be, for some process models, an optional activity (caveat: provided that a process model exists that specifies the general relationships between concepts in a domain). Our hope is that the results of this paper encouraging enough that other software process researchers might try STAR's stochastic search on their seemingly more complex models.

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